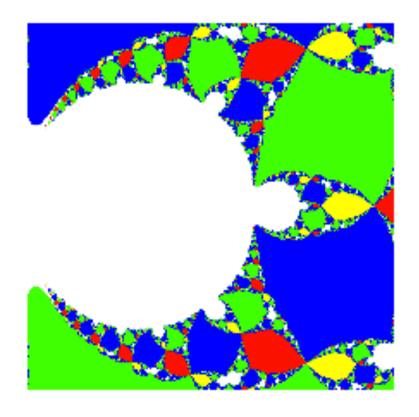
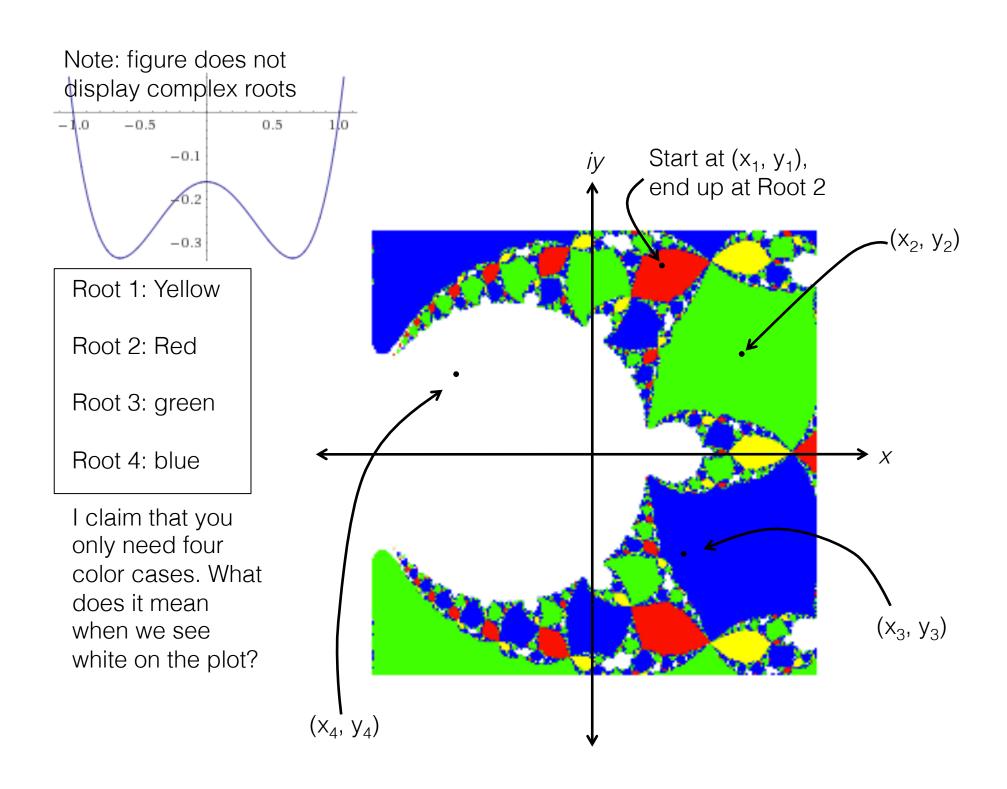
#### Newton Basins



qdrive  $\Delta$  qnewt  $\Delta$  myownpolyder

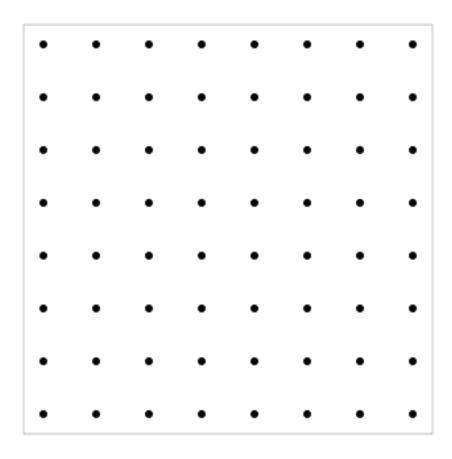


It would be extremely expensive to invoke a for loop and run through every point in the window.

In fact, unless we were working with a finite set of points, the loop would go on forever, and the picture would become more and more detailed

So we make a lattice that covers the plane (window specified by xt and yt) and perform Newton's method on all of the points at once!

Then we have a huge collection (matrix) of the roots that Newton's method finds for each starting point in the lattice.



#### Outline

```
function qdrive

*run qnewt on all 4 quartics*
return
```

```
function qnewt(q,xt,yt,maxiter)

*We will unpack this one*
return
```

function d=myownpolyder(q)

\*Write your own derivative-taking function (one-liner)\*
return

#### qdrive

function qdrive

return

all of the plotting is taken care of in qnewt! The driver really just specifies the quartics and the dimensions of the grid.

## qnewt(q,xt,yt,maxiter)

Where are these specified?

function qnewt(q,xt,yt,maxiter)

- 1. create meshgrid
- 2. take derivative of your quising dq= mypolyder(q)
- 3. Run Newton on entire lattice at once

```
for k=1:maxiter,
   Z = Z - (Z.^2-1).*(Z.^2+0.16)./(4*Z.^3 - 1.68*Z); Why the '.'?
end
```

4. Find roots of q. There is a built-in MATLAB function for this:

$$R = roots(q);$$
 —

5. Use "find" to see which points in Z end up at which root, and plot in the corresponding colors (see next slide).

x = .15:.0025:.55;y = -.15:.0025:.15;[X,Y] = meshgrid(x,y);

Z = X+i\*Y:

What are the numerator and denominator in terms of dq?

We know that there are 4 roots of q. So in what form must R be?

#### plotting in qnewt

R is a 1x4 vector of the roots of q.

We will evaluate each of these roots independently, and see which points in Z ended up at that root. \_\_\_\_ 0.1 is the

0.1 is the tolerance you will use

- 1 [i1,j1] = find(abs(Z-1)<0.1);
- 2. Plot: use indices i1 and j1 to access points in the x-y plane; color those points whatever color you like. Use markersize 1.
  - Hint for accessing points in the x-y plane: where have we discretized the plane/created a lattice? (see slide 8, step 1).
- 1 is an example root from the notes. How can we write each of the roots in terms of R for the four cases?

3. hold on, and repeat for the next 3 roots.

## dq = myownpolyder(q)

$$2z^{4} - 4z^{3} + (2-i)z^{2} - iz + 10$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow$$

$$q = [2 \qquad -4 \qquad (2-i) \qquad -i \qquad 10]$$

$$dq = [8 -12 4-2i -i]$$

How can we automate the process of arriving from q to dq? What same operations are performed *every time*?

# dq = myownpolyder(q)

- -kill the last element of q
- -multiply the first four elements of q by the corresponding exponents [4 3 2 1]