

# Cryptography

Project 7

# Outline

1. decoderdrive
2. decoder
3. downlow
4. downlowinv
5. loglike

# Outline

1. decoderdrive
  - calls decoder once for each message, displays output
2. decoder
  - decodes message using Metropolis Algorithm
3. download
  - letters → numbers
4. downloadinv
  - numbers → letters
5. loglike
  - computes likelihood of your guess given the inputted text (message you're trying to decode)

# Metropolis Algorithm

First: letter pair probabilities (in letterprob.dat, use load) and encoded text (use fileread) need to be imported.

Generate an initial random guess:

```
y = randperm(27)
```

To compare the encoded message to your guess, you need to convert it to numbers

# Metropolis Algorithm

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Generate an initial random guess,  $y = \text{randperm}(27)$ .

Main loop:

- consider a potential guess,  $y_{\text{maybe}}$ , obtained by switching 2 random elements in  $y$

You have two possibilities for the next guess.

Either  $y_{\text{new}} = y_{\text{maybe}}$ , or no change is made ( $y_{\text{new}} = y$ ).

# Metropolis Algorithm

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Main loop: (repeated  $10^4$  or  $10^5$  times)

- consider a potential guess, ymaybe, obtained by switching 2 random elements in y

You have two possibilities for the next guess. Either ynew = ymaybe, or no change is made (ynew = y).

- Compute log likelihood of y and ymaybe.

- (a)  $\text{loglike}(\text{ymaybe}) > \text{loglike}(y)$

- ynew = ymaybe with 100% probability

- (b)  $\text{loglike}(\text{ymaybe}) < \text{loglike}(y)$

- ynew = ymaybe with probability =

- $\exp[-\text{loglike}(y) + \text{loglike}(\text{ymaybe})]$ ,
- otherwise ynew = y (guess doesn't change)

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Display encrypted & decrypted messages

# loglike function

likelihood = loglike(crypt, guess, M)

$$\sum_i \log(M(t_{\sigma(i)}, t_{\sigma(i+1)}))$$

For each pair of subsequent letters in the encrypted message ('crypt'), find your guess for those letters (in 'guess').

Add the log of the corresponding element in M to the sum.



# downlow and lowdown

num = downlow(text) | letter= lowdowninv(num)

use “double”

```
>>s=double('hello')
```

```
s =
```

```
104 101 108 108 111
```

use “char”

```
>> [char(s)]
```

```
ans =
```

```
hello
```