

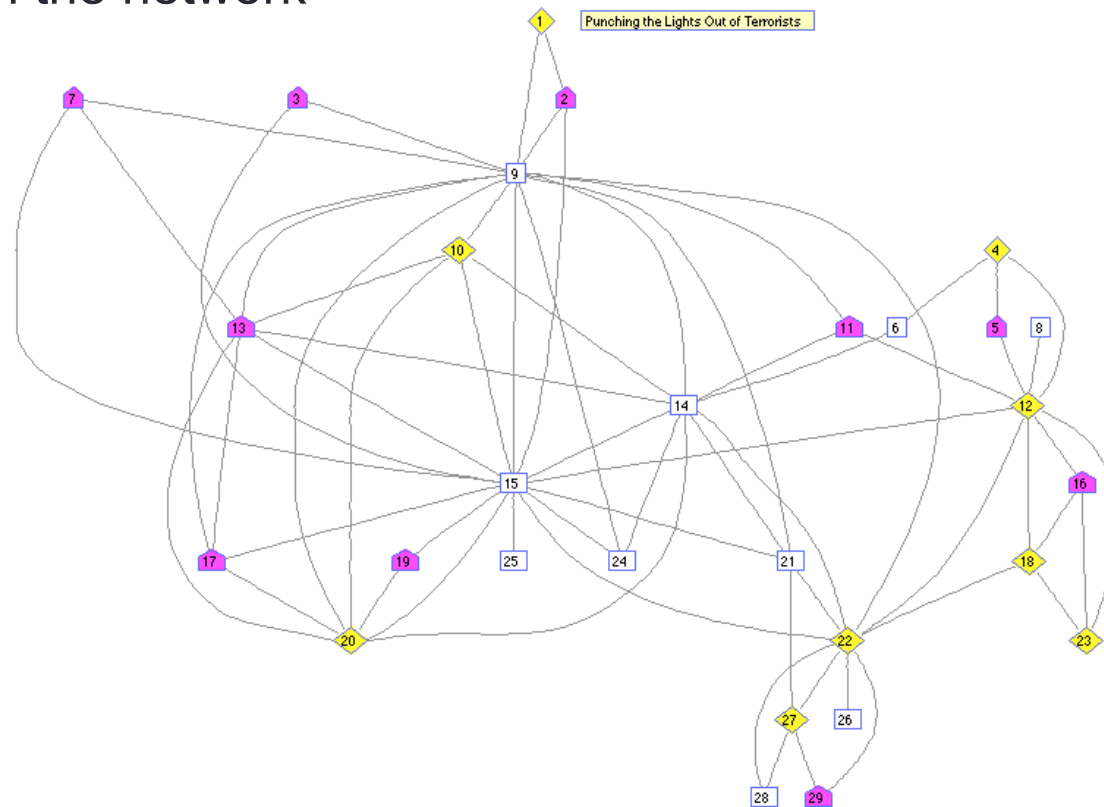


LIGHTS OUT!

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Purpose

- Solve the *Lights Out* puzzle using modular arithmetic
- Our initial condition is the network we used in the Social Networks lab
- Goal: figure out which ‘buttons’ to press to knock out all of the terrorists in the network



Functions

- `Gaussp(A+I,-v)` – puts matrix in upper triangular form
 - $A+I$ is adjacency matrix + identity matrix
 - $-v$ is the initial condition of the network
 - Use mod command to make matrix entries 0 or 1
 - Skip columns with no remaining 1s
 - Delete rows which are all 0s
- `Trisolve(A+I,-v)` – solves for the matrix given initial condition
 - Use mod command to make matrix entries 0 or 1

Modifications

- In gaussp, skip to next column when you encounter a bad column
 - Do not skip down to the next row (might skip entries that need to be row-reduced)

```
function x = gauss(S,f)
n = length(f);
S = [S | f]      Augment S with f
for k=1:n-1      k counts columns
    r = row number, larger than or equal to k,
        with largest value (in magnitude) in column k
    if this largest value is really small then warn the user
    swap row r and row k
    for j=k+1:n
        mix row k into row j in order to eliminate S(j,k)
    end
end
if S(n,n) is really small then warn the user
strip off the changed f, i.e., copy column n+1 of S onto f
x = trisolve(S,f)
return
```

Modular Arithmetic

“e ven”		“o dd”			→/	“e ven”	
“e ven”		“o dd”			“e ven”	“e ven”	
“o dd”		“e ven”			“o dd”	“e ven”	

is the same as

+		0	1			→/	0	1
0		0	1			0	0	0
1		1	0			1	0	1

and

$$\begin{aligned}
 1 + 1 + 1 + 1 + 1 &= 5 \not\equiv 1 \pmod{2} \\
 1 + 1 + 1 + 1 + 1 &= (1 + 1) + (1 + 1 + 1) = 2 + 3 \equiv 0 + 1 \pmod{2} \equiv 1 \pmod{2} \\
 1 + 1 + 1 + 1 + 1 &= 5 \not\equiv (1 + 1 + 1 + 1 + 1) = 5 \not\equiv 1 \pmod{2} \equiv 1 \pmod{2}
 \end{aligned}$$